

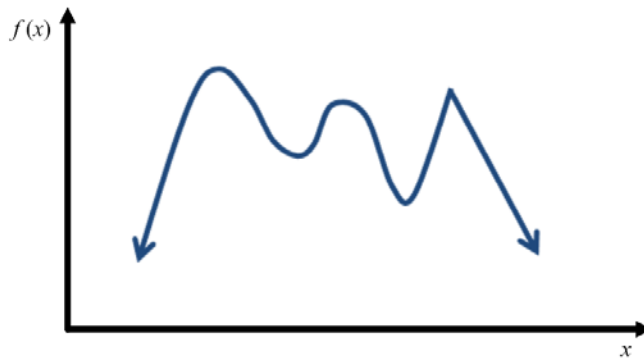
5.1 Extreme Values

CALCULUS

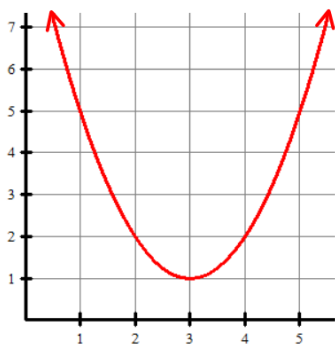
Write your questions here!



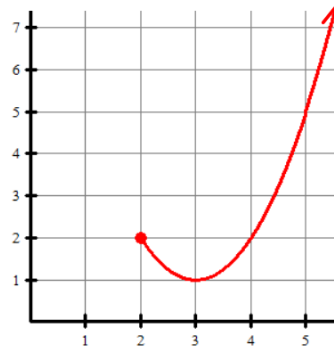
Extrema =



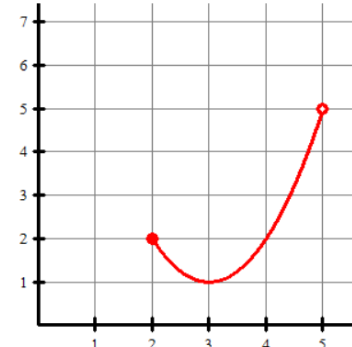
Critical Points =



Domain: $(-\infty, \infty)$



Domain: $[2, \infty)$



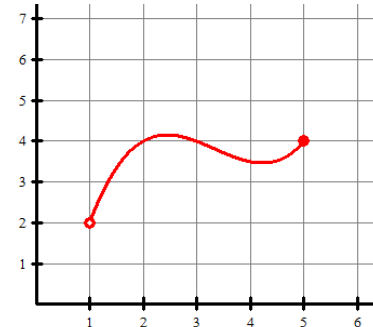
Domain: $[2, 5)$



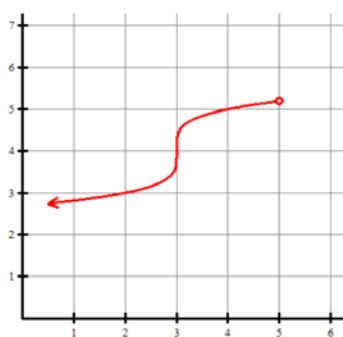
Domain: $[1, 6]$



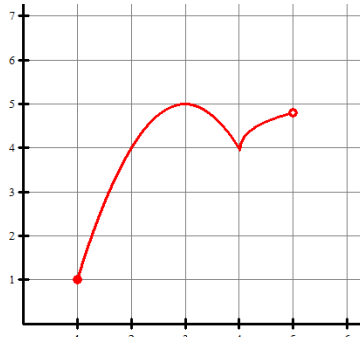
Domain: $(1, 6]$



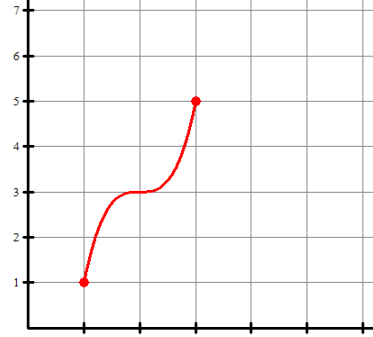
Domain: $(1, 5)$



Domain: $(-\infty, 6]$



Domain: $[1, 5)$



Domain: $[1, 3]$

Extreme Value Theorem

If f is continuous on a closed interval $[a, b]$, then f has both a maximum and minimum value on the interval.

Find the critical points of the function.

$$f(x) = \frac{1}{3}x^3 - 9x + 24$$

$$g(x) = \frac{1}{\sqrt{4-x^2}}$$

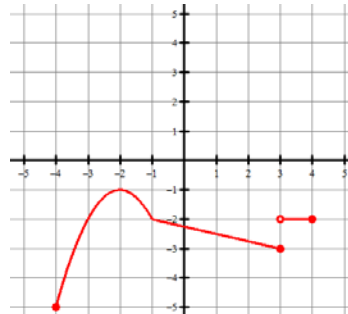
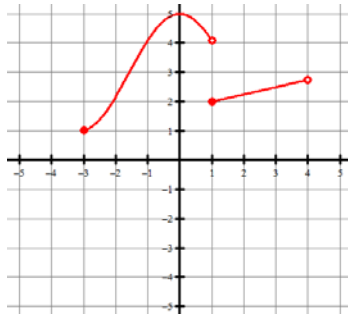
Find the absolute maximum and minimum values of the function on the given interval.

$$f(x) = x^3 - 3x^2 + 1, \quad \left[-\frac{1}{2}, 4\right]$$

$$h(x) = 2x - 3x^{\frac{2}{3}}, \quad [-1, 3]$$



Find the extreme values and where they occur.



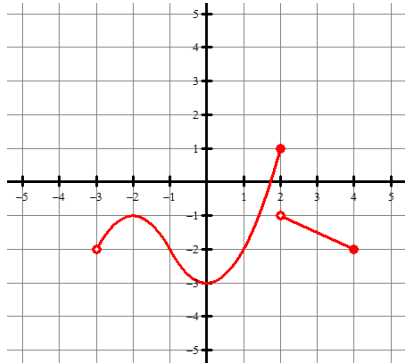
SUMMARY:

Now,
summarize
your notes
here!

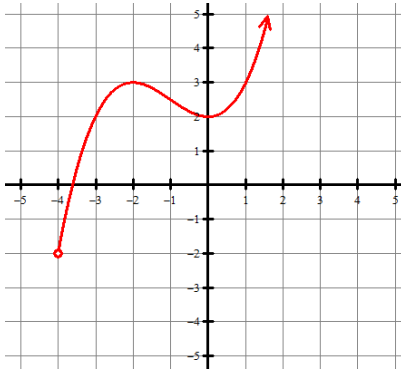


Find the extreme values and where they occur.

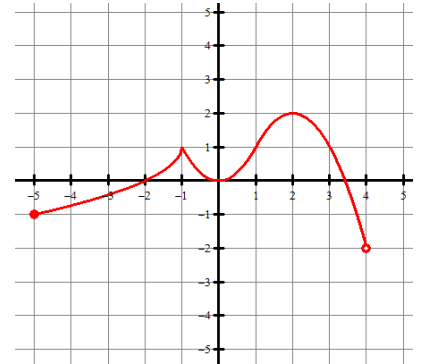
1.



2.

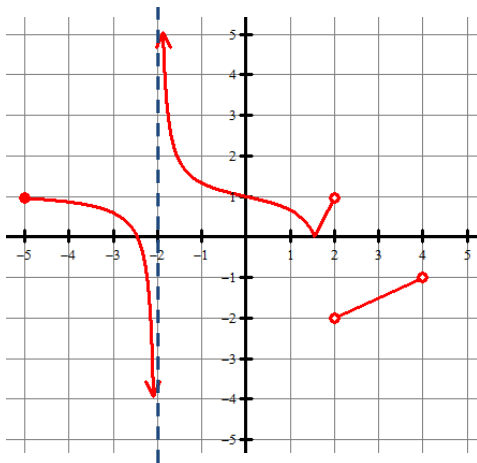


3.



Use the graph of $f(x)$ to answer the following.

4.



Domain:

Absolute max:

$$\lim_{x \rightarrow 2^+} f(x) =$$

Absolute min:

$$\lim_{x \rightarrow -2} f(x) =$$

Local max:

$$\lim_{x \rightarrow 0} f(x) =$$

Local min:

$$f(3) =$$

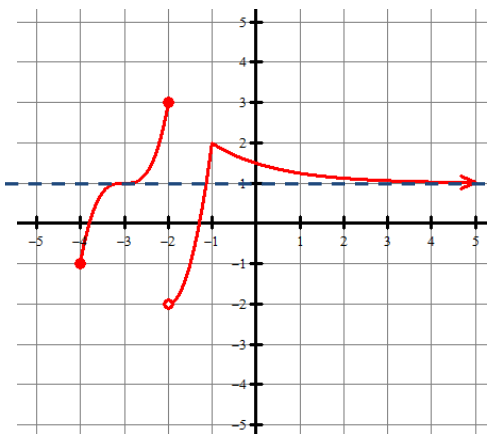
Interval(s) where $f(x)$ increasing

$$f'(3) =$$

Interval(s) where $f(x)$ decreasing

Average rate of change over $[-5, -3]$

5.



Domain:

Global max:

$$\lim_{x \rightarrow -2^+} f(x) =$$

Global min:

$$\lim_{x \rightarrow -2} f(x) =$$

Relative max:

$$\lim_{x \rightarrow \infty} f(x) =$$

Relative min:

$$f(-3) =$$

Interval(s) where $f(x)$ increasing

$$f'(-1) =$$

Interval(s) where $f(x)$ decreasing

Average rate of change over $[-4, -2]$

Find the critical points.

6. $f(x) = 4x^3 - 9x^2 - 12x + 3$

7. $g(t) = \frac{2}{t^2 - 4}$

8. $h(x) = \sqrt[3]{x - 2}$

9. $f(x) = (\ln x)^2$

10. $h(x) = 2 \sin\left(\frac{x}{2}\right)$
where $-2\pi \leq x \leq 2\pi$

11. $g(x) = e^x - x$

Find the absolute maximum and minimum values of the function on the given interval.

12. $f(x) = 1 + (x + 1)^2, \quad [-2, 5]$

13. $f(x) = 2x^3 + 3x^2 + 4 \quad [-2, 1]$

14. $f(x) = x^3 - 12x, \quad [0, 3)$

15. $h(x) = 3x^{\frac{2}{3}} - 2x, \quad [-1, 1]$

Find the absolute maximum and minimum values of the function on the given interval.

16. $g(x) = x^2 + \frac{2}{x}, \quad \left(\frac{1}{2}, 2\right]$

17. $f(x) = \frac{x}{x^2+1}, \quad [-2, 2]$

18. $f(x) = \sin\left(x + \frac{\pi}{4}\right), \quad \left[0, \frac{7\pi}{4}\right]$

19. $g(x) = xe^{2x}, \quad [-1, 1]$



5.1 Extreme Values

TEST PREP

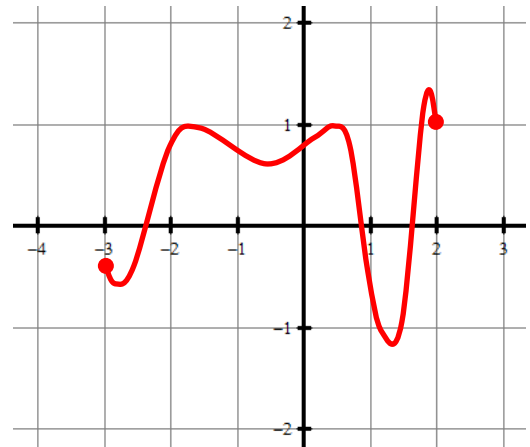
MULTIPLE CHOICE

1. If f is a continuous, decreasing function on $[0,10]$ with a critical point at $(4, 2)$, which of the following statements must be false?
- (A) $f(10)$ is an absolute minimum of f on $[0,10]$.
 - (B) $f(4)$ is neither a relative maximum nor a relative minimum.
 - (C) $f'(4)$ does not exist
 - (D) $f'(4) = 0$
 - (E) $f'(4) < 0$

Questions 2 and 3 refer to the graph shown on the right.

2. Which of the following statements is false?

- (A) $F(-3) + F(2) > 0$
- (B) $F(-1) + F'(-1) > 0$
- (C) $F'(-1) \cdot F''(-1) < 0$
- (D) $F(1) \cdot F'(1) < 0$
- (E) $F(0) \cdot F'(0) > 0$



The graph of F

3. The function F has exactly this many critical numbers.

- (A) 4
- (B) 5
- (C) 6
- (D) 7
- (E) 8

4. Let $x(t) = t^{\frac{2}{3}}$ give the distance of a moving particle from its starting point as a function of time t . For what value of t is the instantaneous velocity of the particle equal to its average velocity over the interval $[0,8]$?

- (A) $\frac{8}{27}$
- (B) $\frac{27}{64}$
- (C) $\frac{64}{27}$
- (D) $\frac{27}{8}$
- (E) $\frac{64}{9}$

5. What is the range of the function $f(x) = \frac{\ln x}{x}$ on the closed interval $[1, e^2]$?

- (A) $f(1) \leq f(x) \leq f(e)$
- (B) $f(1) \leq f(x) \leq f(e^2)$
- (C) $f(2) \leq f(x) \leq f(e)$
- (D) $f(e) \leq f(x) \leq f(e^2)$
- (E) None of these



You will need a graphing calculator for #6



6. Find the value of c that satisfies the Mean Value Theorem for $f(x) = x \sin x$ on $[1,4]$.

- (A) 1.239
- (B) 1.290
- (C) 2.029
- (D) 2.463
- (E) 3.027