

8.4 Area Between Curves (with respect to x)

Calculus

Name: _____

CA #2

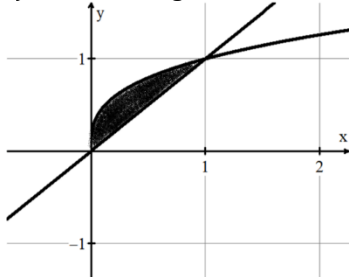
Find the area of the region bounded by the following graphs. Show your work.

1. $y = \sqrt[3]{x}$, $x = 0$, and $y = 2$

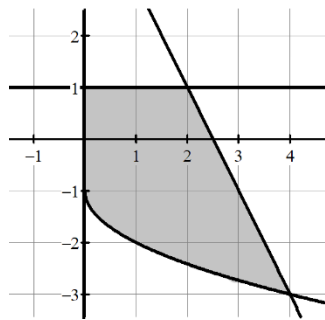
2. $y = x^2$ and $y = 4x - x^2$

Set up an integral(s) that represents the shaded region. Do not solve. Use a calculator if necessary to help find the lower and upper bounds.

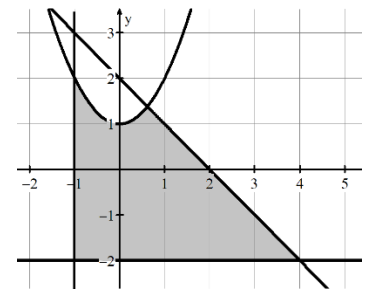
3. $f(x) = \sqrt[3]{x}$, $g(x) = x$



4. $y = -\sqrt{x} - 1$, $y = 1$,
 $y = 5 - 2x$, and $x = 0$

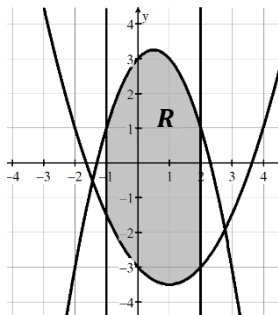


5. $y = x^2 + 1$, $y = -2$,
 $y = 2 - x$, and $x = -1$

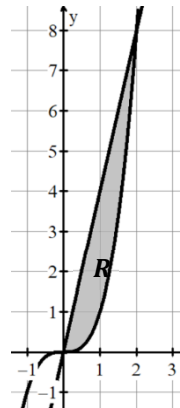


Let R be the region bounded by the given curves as shown in the figure. If the line $x = k$ divides R into two regions of equal area, find the value of k

7. $y = -x^2 + x + 3$, $y = \frac{1}{2}x^2 - x - 3$, $x = -1$, and $x = 2$



8. $y = x^3$ and $y = 4x$



Answers to 8.4 CA #2

1. $\int_0^8 (2 - \sqrt[3]{x}) dx = 4$	2. $\int_0^2 (4x - 2x^2) dx = \frac{8}{3}$	3. $\int_0^1 (\sqrt[3]{x} - x) dx$	4. $\int_0^2 (2 + \sqrt{x}) dx + \int_2^4 (6 - 2x + \sqrt{x}) dx$
5. $\int_{-1}^A (x^2 + 3) dx + \int_A^4 (4 - x) dx$ where $A = 0.618034$	6. $k \approx 1.445$	7. $k \approx 0.5846$	