

Name: \_\_\_\_\_ Date: \_\_\_\_\_

## Unit 4 CA – Contextual Application of Differentiation

1. The position of a particle moving along a coordinate line is  $s(t) = 2t^3 - 6t$ , with  $s$  in meters and  $t$  in seconds. Find the particle's velocity and acceleration at  $t = 6$ .

Find the following. Use L'Hospital's when possible.

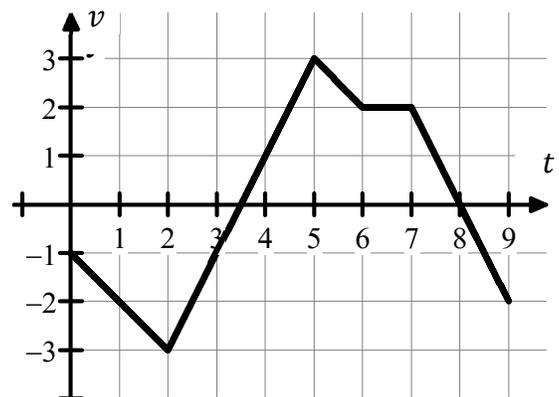
2.  $\lim_{x \rightarrow 0} \frac{x^2}{1 - \cos(3x)}$

3.  $\lim_{x \rightarrow 4} \frac{x^2 + 6x - 40}{4 - x}$

4.  $\lim_{x \rightarrow 3} \frac{x^2 - 2x + 1}{x - 3}$

5. The figure shows the velocity  $v$  of a body moving along a coordinate line in meters per second.

- When does the body reverse direction?
- When is the body moving at a constant speed?
- What is the body's maximum speed?
- At what time interval(s) is the body slowing down?



6. A rocket lifts off at the Kennedy Space Center in Florida. A camera is placed 2000 feet away from the launch pad to film the rocket's ascent. The height of the rocket can be found using  $s(t) = 50t^2$ , where  $s$  is feet and  $t$  is seconds. Find the rate of change in the angle of elevation of the camera at 10 seconds after lift-off.
7. Two roads cross at right angles, one running north/south and the other east/west. Eighty feet south of the intersection is an old radio tower. A car traveling at 50 feet per second passes through the intersection heading east. At how many feet per second is the car moving away from the radio tower 3 seconds after it passes through the intersection?
- (A) 43.65                                      (B) 44.12                                      (C) 44.59
- (D) 56.67                                      (E) 81.76
8. The function  $f(x) = -xe^x + 2$  is concave down at  $x = 0$ .
- a. Find the tangent line of  $f$  at  $x = 0$ .
- b. What is the estimate for  $f(-0.1)$  using the local linear approximation for  $f$  at  $x = 0$ ?
- c. Is it an underestimate or overestimate? Explain.

### Unit 4 Corrective Assignment – Answers

1. $s'(6) = 210$ meters / sec $s''(6) = 72$ meters / sec <sup>2</sup>	2. $\frac{2}{9}$	3. $-14$	4. Does not exist	5a. $t = 3.5$ and $t = 8$ 5b. $(6, 7)$ 5c. 3 meters / sec 5d. $(2, 3.5)$ , $(5, 6)$ and $(7, 8)$
6. Setup: $\tan \theta = \frac{1}{2000}s$  Answer: 0.0689 radians per second	7. B	8a. $y = -x + 2$ 8b. $f(-0.1) \approx 2.1$ 8c. Overestimate because $f(x)$ is concave down.		