

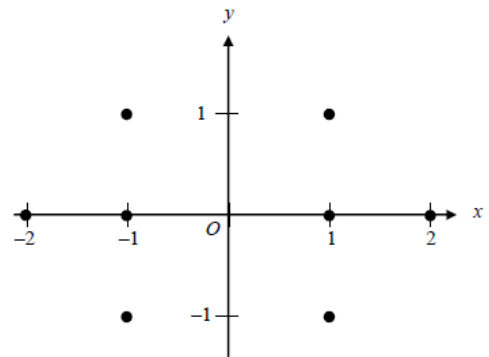
Name: _____ Date: _____ Period: _____

Unit 7 Review – Differential Equations

Reviews do NOT cover all material from the lessons but will hopefully remind you of key points. To be prepared, you must study all packets from Unit 7.

1. Consider the differential equation $\frac{dy}{dx} = \frac{y^2}{x}$, where $x \neq 0$.

a. On the axes provided, sketch a slope field for the given differential equation at the eight points indicated.



b. Find the particular solution $y = f(x)$ to the differential equation with the initial condition $f(1) = -1$.

c. Write an equation for the tangent line to the curve $y = f(x)$ through the point $(1, -1)$. Then use your tangent line equation to estimate the value of $f(1.2)$.

2. The rate of change of the volume, $V(t)$, of water in a swimming pool is directly proportional to the cube root of the volume. If $V = 27 \text{ ft}^3$ when $\frac{dV}{dt} = 5$, what is a differential equation that models this situation?

Find the general solution of the differential equation.

3. $\frac{dy}{dx} = \frac{2x}{y}$

4. $\frac{dy}{dx} = x(y + 4)$

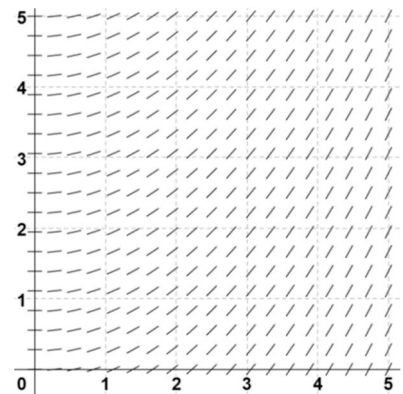
For each differential equation, find the particular solution that passes through the given point.

5. $\frac{dy}{dx} = \frac{18}{6x+3} + \frac{4}{x^3}$; $\left(-\frac{1}{3}, -15\right)$

6. $\frac{dy}{dx} = 2y$ and $y = -0.2$ when $x = 0$

7. A population y grows according to the equation $\frac{dy}{dt} = ky$, where k is a constant and t is measured in years. If the population doubles every 12 years, then what is the value of k ?

8. Explain why the following slope field cannot represent the differential equation $\frac{dy}{dt} = 0.4y$



9. For what value of k , if any, will $y = k \cos(2x) + 3 \sin(4x)$ be a solution to the differential equation $y'' + 16y = -6 \cos(2x)$?