

## 2.2 Definition of the Derivative

Calculus

Name: \_\_\_\_\_

**CA #1**

Find the derivative using limits. If the equation is given as  $y =$ , use Leibniz Notation:  $\frac{dy}{dx}$ . If the equation is given as  $f(x) =$ , use Lagrange Notation:  $f'(x)$ . WRITE SMALL!!

1.  $f(x) = 5x + 1$

2.  $y = 2 + 10x - x^2$

3.  $f(x) = 5x^2 - x$

4.  $f(x) = \sqrt{6x + 5}$

5.  $y = \frac{1}{5-x}$

For each problem, create an equation of the tangent line of  $f$  at the given point. Leave in point-slope.

6.  $f(1) = -5$  and  $f'(1) = 3$

7.  $f(6) = 2$  and  $f'(6) = -8$

8.  $f(x) = x \sin x$   
 $f'(x) = \sin x + x \cos x$ ;  $x = \pi$

$$9. f(x) = \sqrt{5x+1}$$

$$f'(x) = \frac{5}{\sqrt{5x+1}}; x = 7$$

$$10. f(x) = 2x - 3x^2$$

$$f'(x) = 2 - 6x; x = -2$$

$$11. f(x) = \tan(5x)$$

$$f'(x) = 5 \sec^2(5x); x = \frac{\pi}{20}$$

Identify the original function  $f(x)$ , and what value of  $c$  to evaluate  $f'(c)$ .

$$12. \lim_{h \rightarrow 0} \frac{2^{5+h} - 2^5}{h}$$

$$13. \lim_{h \rightarrow 0} \frac{2(6+h)^2 + (6+h) - 3 - (75)}{h}$$

$$14. \lim_{x \rightarrow -3} \frac{(4x^2 + 2x) - (30)}{x+3}$$

$$15. \lim_{x \rightarrow 1} \frac{\frac{1}{10+x} - \frac{1}{11}}{x-1}$$

Answers to 2.2 CA #1

1. $f'(x) = 5$	2. $\frac{dy}{dx} = 10 - 2x$	3. $f'(x) = 10x - 1$	4. $f'(x) = \frac{3}{\sqrt{6x+5}}$	5. $\frac{dy}{dx} = \frac{1}{(5-x)^2}$
6. $y + 5 = 3(x - 1)$	7. $y - 2 = -8(x - 6)$	8. $y = -\pi(x - \pi)$	9. $y - 6 = \frac{5}{6}(x - 7)$	10. $y + 16 = 14(x + 2)$
11. $y - 1 = 10(x - \frac{\pi}{20})$	12. $f(x) = 2^x$ $f'(5)$	13. $f(x) = 2x^2 + x - 3$ $f'(6)$	14. $f(x) = 4x^2 + 2x$ $f'(-3)$	15. $f(x) = \frac{1}{10+x}$ $f'(1)$