UNIT 3 Basic Differentiation

REVIEW

NAME:_____

DATE:_____

Evaluate the limit.

1.
$$\lim_{x \to \infty} \frac{x^3 + 5x^2 - x}{1 - e^x} =$$

2.
$$\lim_{x \to 2} \frac{x^2 + 7x - 18}{x^2 - 2x} =$$

Given f(x) on a given interval [a, b], find a value *c* that satisfies the Mean Value Theorem.

3.
$$f(x) = -x^2 + 4x - 2; [-1, 2]$$

Find *b* and *c* so that f(x) is differentiable at x = 1.

4.
$$f(x) = \begin{cases} 3x^2 + 4x, & x \le 1\\ 2x^3 + bx + c, & x > 1 \end{cases}$$

Find the derivative of the following.				
$5. f(x) = \frac{\sin x}{x^2 + 1}$	6. $g(x) = \sqrt{2x^3 - 4x}$			
7. $y = \frac{x^3 + 4x - 1}{2x}$	8. $h(x) = \cos^2(4x)$			

Find the following

9. $f(x) = x^2 \sin(x)$ $f'\left(\frac{\pi}{2}\right) =$

10.
$$g(x) = \frac{1}{\sqrt{x}}$$

 $g''(x) =$

Write the equation of the tangent line and the normal line at the point given.

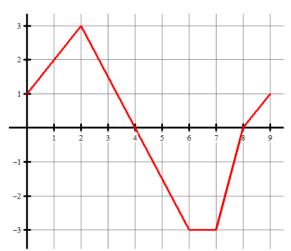
11. $f(x) = 3 \tan x$ at $x = \pi$

Particle Motion

12. The position of a particle moving along a coordinate line is $s(t) = 2t^3 - 6t$, with *s* in meters and *t* in seconds. Find the particle's velocity and acceleration at t = 6.

13. The figure shows the velocity $v = \frac{ds}{dt} = f(t)$ of a body moving along a coordinate line in meters per second.

- a) When does the body reverse direction?
- b) When is the body moving at a constant speed?
- c) What is the body's maximum speed?
- d) At what time interval(s) is the body slowing down?



Use the information to find the following.

14. The table shows the number of stores of a popular US coffee chain from 2000 to 2006. The number of stores recorded is the number at the start of each year, on January 1st.

t (year)	2000	2001	2002	2004	2005	2006
S (stores)	1996	2729	3501	5239	6177	7353

Approximate the instantaneous rate of change in coffee stores per year at the beginning of 2003.



You are allowed to use a graphing calculator for #15



15. The amount A(t) of pain reliever in milligrams in a patient's system after t minutes is given by $A(t) = 8te^{-t/50}$.

- a. Find A(60). Explain what it means in a sentence.
- b. Find A'(60). Explain what it means in a sentence.
- c. Find A(t) = 100. Explain what it means in a sentence.
- d. What is the average rate of change of milligrams from 60 minutes to 180 minutes?
- e. What is the instantaneous rate of change at 180 minutes?
- f. When does A'(t) = 0? What is happening at this point?
- g. Find $\lim_{t\to\infty} A(t)$ Explain what it means in a sentence.

TEST PREP

- 1. A particle is traveling along the *x*-axis. Its position is given by $x(t) = \frac{1-t^2}{t+3}$ at time $t \ge 0$. Find the instantaneous rate of change of *x* with respect to *t* when t = 1.
 - (A) -2
 - (B) $-\frac{1}{2}$
 - (C) 0
 - (D) $\frac{1}{2}$
 - (**D**)
 - (E) 2
- 2. The line 2x y = 9 is tangent to the curve f(x) at the point (4, -1). What is the value of '(4)?
 - (A) –2
 - (B) $\frac{1}{2}$
 - (C) 2
 - (D) 4
 - (E) 9
- 3. If $f(x) = e^x$, which of the following is equal to f'(e)?

(A)
$$\lim_{h \to 0} \frac{e^{x+h}}{h}$$

(B)
$$\lim_{h \to 0} \frac{e^{x+h} - e^e}{h}$$

(C)
$$\lim_{h \to 0} \frac{e^{e+h} - e}{h}$$

(D)
$$\lim_{h \to 0} \frac{e^{e+h} - 1}{h}$$

(E)
$$\lim_{h \to 0} \frac{e^{e+h} - e^e}{h}$$

- 4. The graph of f(x) is shown below. What is the value of f(1) + f'(1) + 2f'(4)?
 - (A) 0
 - (B) 1
 - (C) 2
 - (D) 3
 - (E) 4

