### 10.13 Radius and Interval of Convergence

Calculus
Name:
Find the interval of convergence for each power series.

1. $\sum_{n=1}^{\infty} \frac{(-1)^{n}(x+5)^{n}}{n} \quad$ 2. $\sum_{n=0}^{\infty} \frac{(-1)^{n} x^{2 n}}{n!}$
2. What is the radius of convergence of the power series $\sum_{n=0}^{\infty} \frac{(x-4)^{n}}{4^{n}}$ ?
3. What is the interval of convergence for the power series $\sum_{n=1}^{\infty} \frac{(-1)^{n+1}(x-4)^{n}}{n k^{n}}$, where $k$ is a positive integer?
4. If the power series $\sum_{n=0}^{\infty} a_{n}(x-1)^{n}$ converges at $x=7$ and diverges at $x=-5$, which of the following must be
true?
I. The series converges at $x=6$.
II. The series is centered at $x=1$.
III. $x=7$ is an endpoint
(A) I only
(B) II only
(C) I and II only
(D) I, II, and III

Answers to 10.13 CA \#2

| 1. $-6<x \leq-4$ | 2. $-\infty<x<\infty$ | 3.4 | 4. $4-k<x \leq 4+k$ | 5. D |
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