10.7 Alternating Series Test

Calculus

Name:

1. Explain why the Alternating Series Test does not apply to the series $\sum_{n=1}^{\infty} \frac{(-1)^n \cos(n\pi)}{n^2}$.

- 2. Determine the convergence or divergence of the series $\sum_{n=1}^{\infty} \frac{(-1)^n n}{\ln(n+1)}.$
- 3. Which of the following series converge?

I.
$$\sum_{n=1}^{\infty} \frac{(-1)^n}{4^n}$$
 II. $\sum_{n=1}^{\infty} \frac{(-1)^n}{\pi^n}$ III. $\sum_{n=1}^{\infty} \frac{(-1)^n n^2}{1+n^2}$

4. Which of the following statements are true about the series
$$\sum_{n=1}^{\infty} \frac{(-1)^n n!}{(2n-1)!}?$$
I. The series is alternating.
II. $|a_{n+1}| \le |a_n|$ for $n \ge 1$.
III.
$$\lim_{n \to \infty} a_n = 0$$

A. I only B. I and II only C. I and III only D. I, II, and III

5. Which of the following statements is true?

A.
$$\sum_{n=1}^{\infty} \frac{(-1)^n (1-n)}{n}$$
 converges by the Alternating Series Test.
B.
$$\sum_{n=1}^{\infty} \frac{(-1)^n (n+1)}{2n}$$
 converges by the Alternating Series Test.
C.
$$\sum_{n=1}^{\infty} \frac{(-1)^n n^2}{4\sqrt{n}}$$
 converges by the Alternating Series Test.
D.
$$\sum_{n=1}^{\infty} \frac{(-1)^n 2\sqrt{n}}{n}$$
 converges by the Alternating Series Test.

Answers to 10.7 CA #1

| 1. The Alternating Series Test of not apply because the series not alternating. | | 3. B | 4. D | 5. D |
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