

2.2 Defining the Derivative

Calculus

Name: _____

CA #1

Find the derivative using limits. If the equation is given as $y =$, use Leibniz Notation: $\frac{dy}{dx}$. If the equation is given as $f(x) =$, use Lagrange Notation: $f'(x)$. **WRITE SMALL!!**

1. $y = x^2 + 2x - 9$

2. $f(x) = \frac{1}{5-x}$

3. $y = \sqrt{4x - 1}$

For each problem, create an equation of the tangent line of f at the given point.

4. $f(1) = -5$ and $f'(1) = 3$

5. $f(x) = x \sin x$
 $f'(x) = \sin x + x \cos x$; $x = \pi$

6. $f(x) = \sqrt{5x + 1}$
 $f'(x) = \frac{5}{\sqrt{5x+1}}$; $x = 7$

For each problem, use the information given to identify the meaning of the two equations in the context of the problem. Write in full sentences!

7. $p(h)$ is the number of people standing in line at a popular amusement park and h is the number of hours since the park opened.
 $p(2) = 2005$ and $p'(3) = 250$

8. $W(t)$ is the volume of water (in liters) in a backpack during a hike and t is the number of minutes passed since the hike began.
 $W(30) = 2.1$ and $d'(90) = -0.07$

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|--|------------------------|----------------------------|--|------------------------|---------------------------------|
| 1. $2x + 2$ | 2. $\frac{(5-x)^2}{1}$ | 3. $\frac{\sqrt{4x-1}}{2}$ | 4. $y + 5 = 3(x - 1)$ | 5. $y = -\pi(x - \pi)$ | 6. $y - 6 = \frac{6}{5}(x - 7)$ |
| 7. After 2 hours, there are 2005 people in line. On the 3rd hour, the number of people in line is increasing by 250 people per hour. | | | 8. After 30 minutes, 2.1 liters of water is in the backpack. At the 90-minute mark, the water is decreasing at a rate of 0.07 liters per minute. | | |