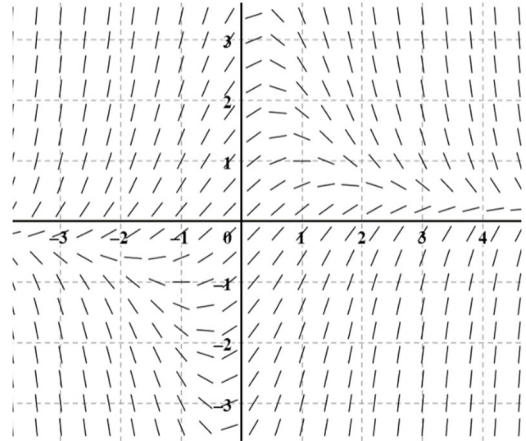


Write your questions and thoughts here!

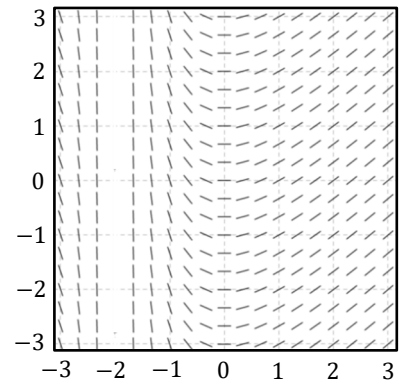
Identify the particular solution that goes through a point.

1. The figure to the right shows the slope for the differential equation $\frac{dy}{dx} = 1 - xy$.
 - a. Sketch the graph of a particular solution that contains $(0, 2)$. Label this point as Point A.
 - b. Sketch the graph of a particular solution that contains $(-1, -2)$. Label this point as Point B.

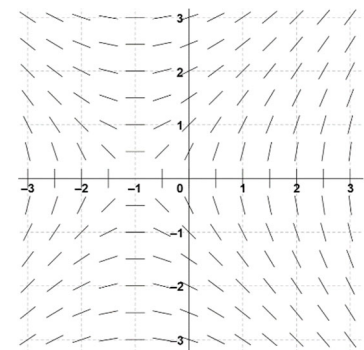


2. The slope field for a certain differential equation is shown to the right. Which of the following could be a solution to the differential equation with the initial condition $y(0) = 0$?

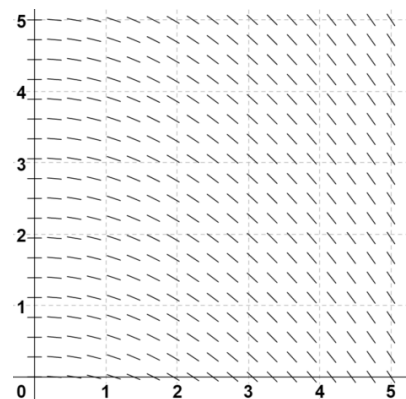
- (A) $y = \frac{x}{x^2-4}$ (C) $y = e^{x+2}$
- (B) $y = \frac{\tan x}{2+x}$ (D) $y = \frac{x^2}{2+x}$



3. Consider the differential equation $\frac{dy}{dx} = \frac{x+1}{y}$ and its slope field shown. Describe all points in the xy -plane, $y \neq 0$, for which $\frac{dy}{dx} = -1$.



4. Explain why the following could not be a slope field for the differential equation $\frac{dy}{dt} = -0.3y$



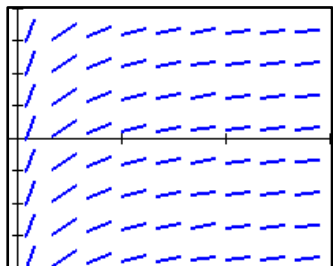
7.4 Reasoning Using Slope Fields

Practice

Calculus

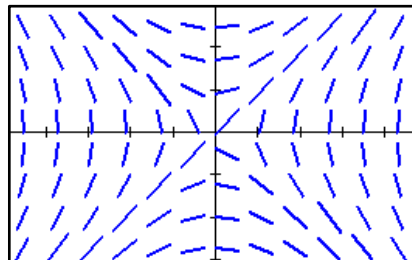
The slope field from a certain differential equation is shown for each problem. The multiple choice answers are either differential equations OR a specific solution to that differential equation.

1.



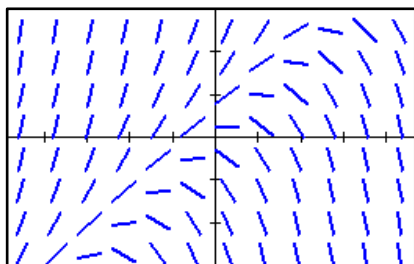
- (A) $y = \ln x$ (D) $y = \cos x$
 (B) $y = e^x$ (E) $y = x^2$
 (C) $y = e^{-x}$

2.



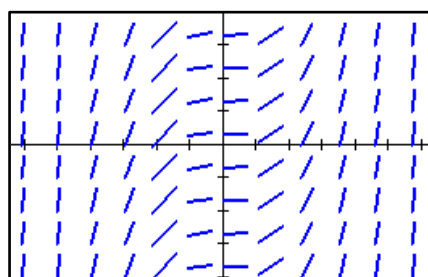
- (A) $\frac{dy}{dx} = x + y$ (D) $\frac{dy}{dx} = (x - 1)y$
 (B) $\frac{dy}{dx} = \frac{x}{y}$ (E) $\frac{dy}{dx} = x(y - 1)$
 (C) $\frac{dy}{dx} = \frac{y}{x}$

3.



- (A) $\frac{dy}{dx} = y - x$ (D) $\frac{dy}{dx} = y(x - 1)$
 (B) $\frac{dy}{dx} = -\frac{x}{y}$ (E) $\frac{dy}{dx} = x(y - 1)$
 (C) $\frac{dy}{dx} = -\frac{y}{x}$

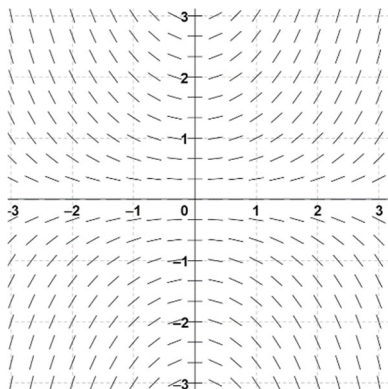
4.



- (A) $y = \sin x$ (D) $y = \frac{1}{6}x^3$
 (B) $y = \cos x$ (E) $y = \frac{1}{4}x^4$
 (C) $y = x^2$

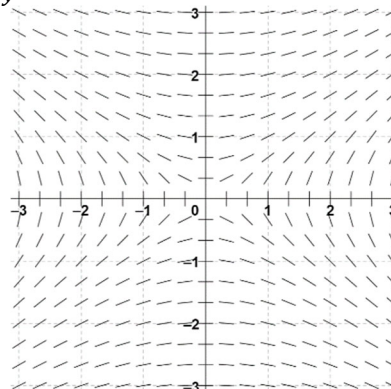
For each slope field, plot and label the points A and B and sketch the particular solution that passes through each of those points. (Two separate solutions for each slope field.)

5. $\frac{dy}{dx} = \frac{xy}{2}$



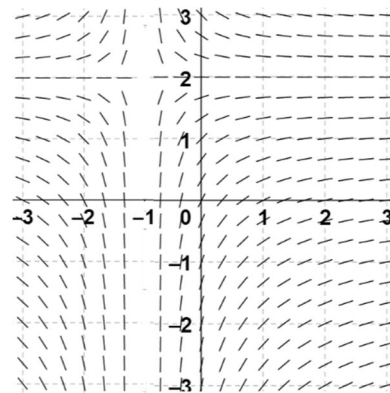
Point A: (0, 1)
 Point B: (-2, -1)

6. $\frac{dy}{dx} = \frac{x}{2y}$



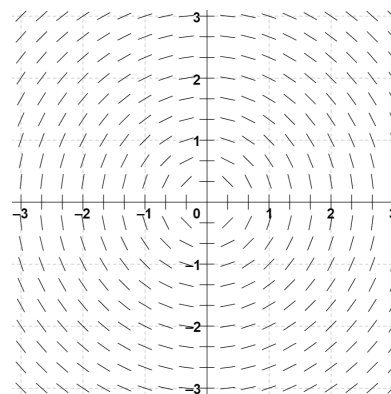
Point A: (0, 1)
 Point B: (-2, 0)

7. The slope field for a certain differential equation is shown. Which of the following could be a solution to the differential equation with initial condition $y(2) = 0$?



- (A) $y = \frac{2x-4}{x+1}$
 (B) $y = \frac{4}{x+1} - 2$
 (C) $y = \ln|1-x|$
 (D) $y = \frac{3x^2}{x+1} - 6$

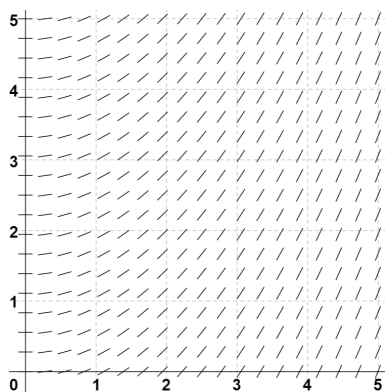
8. The slope field for a certain differential equation is shown. Which of the following could be a solution to the differential equation with the initial condition $y(0) = 1$?



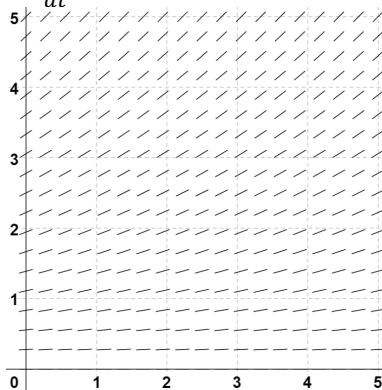
- (A) $y = \frac{x}{y} + 1$
 (B) $y = -\frac{x}{y} + 1$
 (C) $x^2 + (y+1)^2 = 4$
 (D) $x^2 + y^2 = 1$

For each problem below a slope field and a differential equation are given. Explain why the slope field CANNOT represent the differential equation.

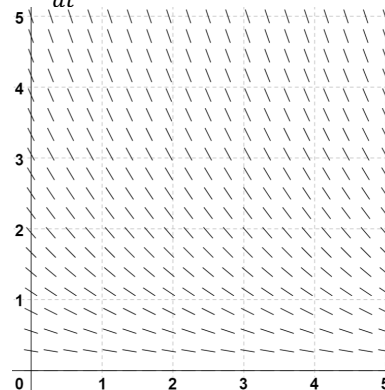
9. $\frac{dy}{dt} = 0.5y$



10. $\frac{dy}{dt} = -0.2y$

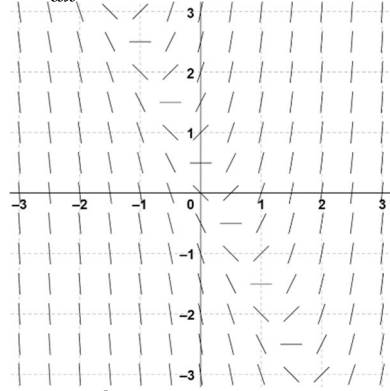


11. $\frac{dy}{dt} = 0.6y$



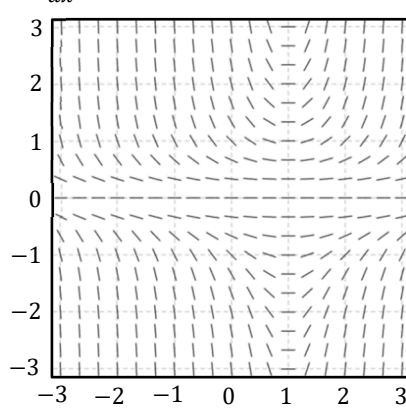
Consider the differential equation and its slope field. Describe all points in the xy -plane that match the given condition.

12. $\frac{dy}{dx} = 2y + 4x - 1$



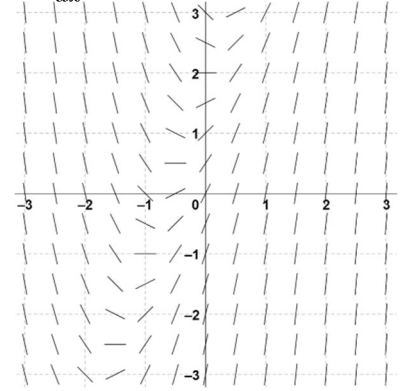
When is $\frac{dy}{dx}$ positive?

13. $\frac{dy}{dx} = y^2(x - 1)$



When are the slopes nonnegative?

14. $\frac{dy}{dx} = 3x - y + 2$

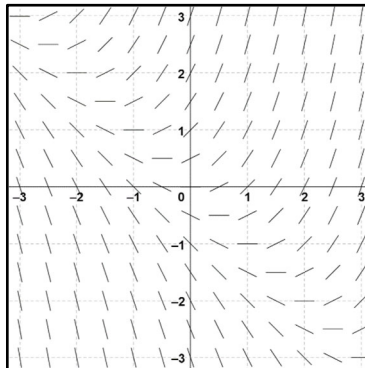


When does $\frac{dy}{dx} = 1$?

7.4 Reasoning Using Slope Fields

Test Prep

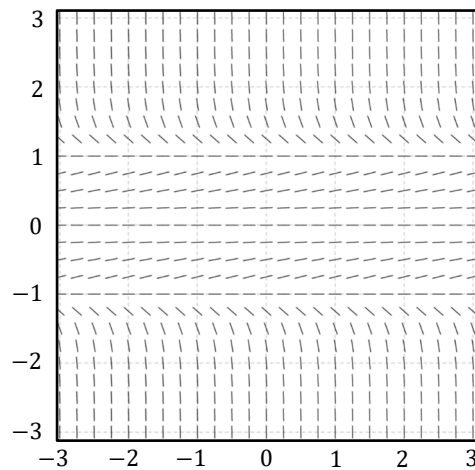
15.



The slope field for a certain differential equation is shown above. Which of the following statements about a solution $y = f(x)$ to the differential equation must be false?

- (A) The graph of the particular solution that satisfies $f(2) = -2$ has a relative minimum at $x = 2$.
- (B) The graph of the particular solution that satisfies $f(-1) = -1$ is concave up on the interval $-2 < x < 1$.
- (C) The graph of the particular solution that satisfies $f(1) = -2$ is linear.
- (D) The graph of the particular solution that satisfies $f(-1) = 2$ is concave up on the interval $-3 < x < 3$.

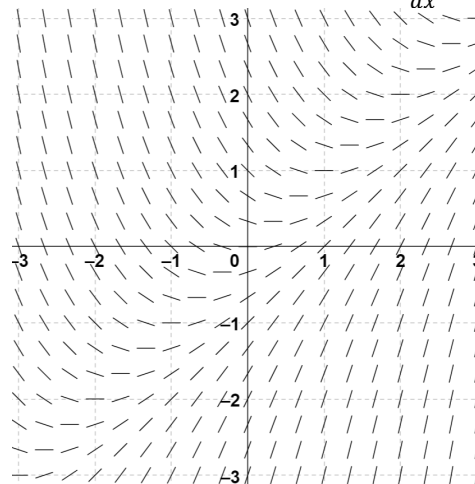
16.



Shown above is a slope field for the differential equation $\frac{dy}{dx} = y^2(1 - y^2)$. If $y = f(x)$ is the solution to the differential equation with initial condition $f(1) = 2$, then $\lim_{x \rightarrow \infty} f(x)$ is

- (A) $-\infty$ (B) -1 (C) 0 (D) 1 (E) ∞

17. The figure below shows the slope field for the differential equation $\frac{dy}{dx} = x - y$



- Sketch the graph of a particular solution that contains $(-1, -1)$. Label this point as Point A.
- Sketch the graph of a particular solution that contains $(1, -1)$. Label this point as Point B.
- State a point where $\frac{dy}{dx} = 0$. Find $\frac{d^2y}{dx^2}$ and use it to verify if your point is a max or min.