9.4 Derivatives of Vector-Valued Functions Notes Calculus Vector basics: Write your questions and thoughts here! • Vectors have magnitude (length) and direction. Vectors can be represented by directed line segments. • Vectors are equal if they have the same direction and magnitude. • Magnitude is designated by ||v||• Vectors have a horizontal and vertical component. • Component form of a vector is $\langle x, y \rangle$ • 1. Find the component form and magnitude of the vector that has an initial point of (1,2) and terminal point (5,4). Component form: Magnitude: **Vector-Valued Functions**: $r(t) = \langle f(t), g(t) \rangle$ where f(t) and g(t) are the component functions with the parameter t. **Differentiation of Vector-Valued Functions** If $r(t) = \langle f(t), g(t) \rangle$ then Properties of the derivative for vector-valued functions $\frac{d}{dt}[r(t) \cdot s(t)] = r'(t)s(t) + r(t)s'(t)$ $\frac{d}{dt}[c \cdot r(t)] = c \cdot r'(t)$ $\frac{d}{dt} \big[r\big(s(t) \big) \big] = r'\big(s(t) \big) \cdot s'(t)$ $\frac{d}{dt}[r(t)\pm s(t)] = r'(t)\pm s'(t)$ 1. $r(t) = \langle 2t^2 + 4t + 1, 3t^3 - 4t \rangle$ then 2. $r(t) = \langle t^3 + 5, 2t \rangle$ find $\frac{d}{dt}r(2t)$ r'(t) =

3. The path of a particle moving along a path in the *xy*-plane is given by the vector-valued function, $f(t) = \langle t^2, \sin t \rangle$. Find the slope of the path of the particle at $t = \frac{3\pi}{4}$.

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Each problem contains a vector-valued function. Fin 1. $f(t) = \langle 4t^3 + 2t^2 + 7t, 4t^2 + 3t \rangle$, then $f'(t) =$	d the given first or second derivative.
1. $f(t) = \langle 4t^3 + 2t^2 + 7t, 4t^2 + 3t \rangle$, then $f'(t) =$	2. $f(t) = \langle 3 \sin 2t, 4 \cos 3t \rangle$, then $f'\left(\frac{\pi}{6}\right) =$
3. $f(t) = \langle 3e^{2t}, 5e^{4t} \rangle$, then $f''(t) =$	4. $f(t) = \langle t^{-2}, (t+1)^{-1} \rangle$, then $f''(-2) =$
5. $f(t) = \langle e^t + e^{-t}, e^t - e^{-t} \rangle$, then $f'(t) =$	6. $f(t) = (2 \sin 4t, 2 \cos 3t)$, then $f'(t) =$
7. $f(t) = \langle t \sin t, t \cos t \rangle$, then $f'\left(\frac{\pi}{2}\right) =$	8. $f(t) = \langle 3t^2 + 6t + 1, 4t^3 - 2t^2 + 6t \rangle$, then f'(1) =

9. The path of a particle moving along a path in the xy-plane is given by the vector-valued function, $f(t) = \langle t^3 + 2t^2 + t, 2t^3 - 4t \rangle$. Find the slope of the path of the particle at t = 3.

10. The position of a particle moving in the *xy*-plane is defined by the vector-valued function, $f(t) = \langle t^3 - 6t^2, 2t^3 - 9t^2 - 24t \rangle$. For what value of $t \ge 0$ is the particle at rest?

Test Prep

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- 11. Calculator active. The path of a particle moving along a path in the *xy*-plane is given by the vector-valued function f and f' is defined by $f'(t) = \langle t^{-1}, 2ke^{kt} \rangle$ where k is a positive constant. The line y = 4x + 5 is parallel to the line tangent to the path of the particle at the point where t = 2. What is the value of k?

12. At time $t, 0 \le t \le 2\pi$, the position of a particle moving along a path in the *xy*-plane is given by the vectorvalued function, $f(t) = \langle t \sin t, \cos 2t \rangle$. Find the slope of the path of the particle at time $t = \frac{\pi}{2}$.