

9.6 Motion using Parametric and Vector-Valued Functions

Calculus

Name: _____

CA #1

1. A particle moving along a curve in the xy -plane has position $(x(t), y(t))$, at time $t \geq 0$, where $\frac{dx}{dt} = 3 \cos(\pi t)$ and $\frac{dy}{dt} = 3t^2$. Find the speed of the particle at time $t = 2$.
2. For time $t \geq 0$, the position of a particle moving in the xy -plane is given by the parametric equations $x(t) = t + t^2$ and $y(t) = (3t + 1)^{-1}$. What is the acceleration vector of the particle at time $t = 1$?
3. For time $t \geq 0$, the position of a particle moving in the xy -plane is given by the vector $\langle 2t^{-2}, e^t \rangle$. What is the velocity vector of the particle at time $t = 3$.
4. **Calculator active.** The position of a particle at time $t \geq 0$ is given by $x(t) = \frac{\sqrt{t+1}}{3}$ and $y(t) = t^2 + 1$. Find the total distance traveled by the particle from $t = 0$ to $t = 2$.
5. **Calculator active.** The velocity vector a particle moving in the xy -plane has components given by $\frac{dx}{dt} = \sin 2t$ and $\frac{dy}{dt} = e^{\cos t}$. At time $t = 2$, the position of the particle is $(3, 2)$. What is the x -coordinate of the position vector at time $t = 3$?

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| 1. $\sqrt{153}$ | 2. $\langle 2, \frac{32}{9} \rangle$ | 3. $\langle -\frac{27}{4}, e^3 \rangle$ | 4. 4.023 | 5. 2.193 |
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Answers to 9.6 CA #1