# Mid-Unit 1 Corrective Assignment - Limits and Continuity 

A child's height can be modeled by the function $h$, where $h(a)$ gives the height in inches and $a$ gives the child's age in years for $0 \leq a \leq 18$. The graph of the function $h$ is shown to the right.

1. Draw a tangent line at $a=9$.
2. Give a rough estimate of the instantaneous rate of change at $a=9$.

3. Give an example of how to calculate a rate of change that would give a close

Years estimate to the rate of change for $a=17$.

A house loan is being paid off each month. The interest being paid each month $m$ can be modeled by $I$, where $I(m)$ is the interest payment and $m$ is the month for $0 \leq m \leq 360$.
4. What does $I(3)$ represent?
5. What does $\frac{I(3)-I(1)}{3-1}$ represent?
6. What does $\frac{I(4)-I(3.999)}{4-3.999}$ represent?

Give the value of each statement. If the value does not exist, write "does not exist" or "undefined." 7.
a. $\lim _{x \rightarrow 3^{-}} f(x)=$
b. $f(-1)=$
c. $\lim _{x \rightarrow-3} f(x)=$
d. $\lim _{x \rightarrow-1} f(x)=$
e. $f(-3)=$
f. $\lim _{x \rightarrow 3^{+}} f(x)=$
g. $f(3)=$
h. $\lim _{x \rightarrow 0} f(x)=$
i. $f(-4)=$


Sketch a graph of a function $h$ that satisfies all of the following conditions.
8.
a. $\lim _{x \rightarrow 3} h(x)=h(-2)=1$
b. $h$ is constant on $-2<x<3$ and decreasing everywhere else.
c. $h(3)$ is undefined.
d. $\lim _{x \rightarrow-2^{-}} h(x)<\lim _{x \rightarrow-2^{+}} h(x)$

9. According to the table, what is value of $\lim _{x \rightarrow-3} f(x)$ ?

| $x$ | -3.4 | -3.001 | -2.999 | -2.7 |
| :---: | :---: | :---: | :---: | :---: |
| $f(x)$ | 7.7 | 7.999 | 8.001 | 8.18 |

10. If $f(x)=\left\{\begin{array}{cc}x^{2}-1, & x \leq 1 \\ \ln x & 1<x \leq e, \text { find the following: } \\ \sqrt{x}, & x>e\end{array}\right.$
a. $\lim _{x \rightarrow e^{-}} f(x)=$
b. $\lim _{x \rightarrow 1} f(x)=$
c. $\lim _{x \rightarrow e} f(x)=$
d. $f(e)=$

## Evaluate the limit.

11. $\lim _{x \rightarrow 1} \frac{x^{2}-2 x-15}{x+3}$

$$
\text { 12. } \lim _{x \rightarrow 2} \frac{x^{2}+2 x-8}{x-2}
$$

13. $\lim _{x \rightarrow-2} \frac{x+2}{x^{2}-4}$
14. $\lim _{x \rightarrow 0} \frac{1-\cos (2 x)}{5 x}$
15. $\lim _{x \rightarrow 2} \frac{\sqrt{x+2}-2}{x-2}$
16. $\lim _{x \rightarrow 0} \frac{\frac{1}{x+8}-\frac{1}{8}}{x}$
17. $\lim _{x \rightarrow-4^{+}} \frac{|x+4|}{x+4}$
18. Let $f$ be a function where $\lim _{x \rightarrow 5} f(x)=6$. Which of the following could represent the function $f$ ?

| I.$f(x)=\left\{\begin{array}{cc} \frac{x^{2}-4 x-5}{x-5}, & x \neq 5 \\ 1, & x=5 \end{array}\right.$ | II. |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $x$ | 4.8 | 4.9 | 4.999 | 5 | 5.001 | 5.1 | 5.2 |
|  | $f(x)$ | 6.2 | 6.1 | 6.001 | -2 | 5.999 | 5.9 | 5.8 |


(A) I only
(B) II only
(C) III only
(D) I and II only
(E) I and III only
19. If $f$ is a piecewise linear function such that $\lim _{x \rightarrow 9} f(x)$ does not exist, which of the following could be representative of the function $f$ ?
I.
$f(x)=\left\{\begin{array}{r|l|l|c|c|c|c|c|}2 x-1, & x<9 \\
\frac{1}{3} x+14, & x>9\end{array}\right.$

| $x$ | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 |  |  |  |  |
| $f(x)$ | 3 | $\frac{10}{3}$ | $\frac{11}{3}$ | -3 | 8 |
| 12 | 16 |  |  |  |  |


(A) I only
(B) II only
(C) III only
(D) I and III only
(E) none
20. Let $f$ and $g$ be the functions defined by $f(x)=\frac{8-8 \cos x}{x^{2}}$ and $g(x)=x^{2} \cos \left(\frac{1}{x}\right)$ for $x \neq 0$. The following inequalities are true for $x \neq 0$. State whether each inequality can be used with the squeeze theorem to find the limit of the function as $x$ approaches 0 ?
I. $4-x^{2} \leq f(x) \leq 4$
II. $-x^{2}-1 \leq g(x) \leq 1+x^{2}$
III. $-x^{2} \leq g(x) \leq x^{2}$
(A) I only
(B) II only
(C) III only
(D) I and II only
(E) I and III only
21. The function $f$ is continuous and increasing for $x \geq 0$. The table gives values of $f$ at selected values of $x$.

| $x$ | 6.5 | 6.999 | 7.001 | 7.5 |
| :---: | :---: | :---: | :---: | :---: |
| $f(x)$ | -6.5 | -6.001 | -5.999 | -5.5 | Approximate the value of $\lim _{x \rightarrow 7} 5 e^{f(x)}$.

## ANSWERS to Mid-Unit 1 Corrective Assignment



